Every student should understand and use all concepts and skills from the previous grade levels. The standard is designed so that new learning builds on preceding skills. Communication, Problem-solving, Reasoning & Proof, Connections, and Representation are the process standards that are embedded throughout the teaching and learning of all mathematical strands.

Strand 1: Number and Operations

Number sense is the understanding of numbers and how they relate to each other and how they are used in specific context or real-world application. It includes an awareness of the different ways in which numbers are used, such as counting, measuring, labeling, and locating. It includes an awareness of the different types of numbers such as, whole numbers, integers, fractions, and decimals and the relationships between them and when each is most useful. Number sense includes an understanding of the size of numbers, so that students should be able to recognize that the volume of their room is closer to 1,000 than 10,000 cubic feet. Students develop a sense of what numbers are, i.e., to use numbers and number relationships to acquire basic facts, to solve a wide variety of real-world problems, and to estimate to determine the reasonableness of results.

Concept 1: Number Sense

Understand and apply numbers, ways of representing numbers, and the relationships among numbers and different number systems.

In Grade 3, students build on their previous work with numbers and deepen their understanding of place value in various contexts. They extend their understanding of the base ten number system to larger numbers and apply this understanding by representing numbers in various equivalent forms. Students develop an understanding of the meanings and uses of fractions. They solve problems that involve comparing and ordering fractions and learn to represent fractions in different ways.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Express whole numbers through six digits using and connecting multiple representations.	Connections: M03-S1C1-02, M03-S1C1-03, M03-S1C2-01, M03-S1C2-03, M03-S2C1-01,	Use models, pictures, symbols, spoken and written words, and expanded notation.
Lesson 3 (identify, read and write 2-digit numbers) Lesson 22 (regrouping tens and ones) Lesson 27 (identify, read and write 3-digit numbers)	M03S3C2-02, M03-S3C3-01	Models may include money, place value charts, or physical objects such as base ten blocks.
Lesson 41 (3-digit numbers in expanded form) Lesson 56, 57 (number sentences for equivalent groups)		Continued on next page

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Grade 3

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
Lesson 59 (identifying quotients) Lesson 64 (4-digit numbers w/ base-10 blocks, models, pictures) Lesson 65-2 (reading temperatures) Lesson 76 (adding 3-digit numbers) Lesson 76 (adding 3-digit numbers) Lesson 77 (arding money amounts to \$1000) Lesson 78 (writing money amounts to \$1000) Lesson 84 (number of days in a year) Lesson 87 (arrays) Lesson 90-1 (divide by 2 and 5) Lesson 90-1 (divide by 2 and 5) Lesson 91 (subtract 2 & 3-digit numbers with money) Lesson 95-1 (X3 facts) Lesson 100-1 (X4 facts) Lesson 103 (read/write 5-digit numbers) Lesson 104 (4-digit numbers in expanded form) Lesson 105-1 (multiplication and division fact families) Lesson 106 (writing checks up to \$99,999.99) Lesson 107 & 108 (division story problems) Lesson 109 (multiplying multiples of 10, 100, 1000) Lesson 123 (negative numbers) Lesson 124 (dividing 2-digit numbers) Lesson 129 (coordinate plane) Lesson 134 (place value to millions)		 Examples: If the diagram represents the number 231, how would you represent the number 4,521? 231 The US Census Bureau estimates that the number of children between the ages of 5 and 13 in Arizona in 2006 was seven hundred ninety-one thousand, nine hundred thirty-one. What is this number written in numeric form?
PO 2. Compare and order whole numbers through six digits by applying the concept of place value. Lesson 2 (ordering birth dates) Lesson 3 (identifying digits) Lesson 7 (ordering 2 digit numbers)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols.	Use comparative language and symbols (<, >, =, ≠).

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: Lesson 8 (order 2-digit numbers) Lesson 13 (comparing values of sets of coins) Lesson 34 (ordering 3-digit numbers) Lesson 47 (comparison symbols) Lesson 51 (constructing number line) Lesson 77 (ordinal numbers) Lesson 120-2 (ordering factors) Lesson 123 (negative numbers) Lesson 128 (adding positive and negative numbers)	Connections: M03-S1C1-01, M03-S1C1-04, M03-S1C3-01, M03-S2C1-02, M03-S2C4-02, M03-S3C3-01	
PO 3. Count and represent money using coins and bills to \$100.00. Lesson 13 (comparing values of sets of coins) Lesson 23 (counting dimes, nickels, pennies) Lesson 28 (writing money w/ \$ and cent signs) Lesson 36 (counting quarters) Lesson 76 (adding 3-digit numbers) Lesson 79 (select coins for a given amount) Lesson 91 (\$1's, \$10's and \$100 bills) Lesson 102 (making change from \$1) Lesson 122 (dividing with money)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. Connections: M03-S1C1-01, M03-S1C2-01, M03-S1C2-02, SS03-S5C2-01, SS03-S5C5-01	

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Performance Objectives	Process Integration &	Explanations and Examples
	Connections	
Students are expected to:		
PO 4. Sort whole numbers into sets and justify the sort.	M03-S5C2-06. Summarize mathematical information,	Numbers may be sorted into categories such as even and odd, magnitude (number between 1-9, numbers
Math Meetings 10 - 31, and periodically thereafter Lesson 9 (identify odd & even)	explain reasoning, and draw conclusions.	between 10-99, etc.), multiples of 5, digits in the numbers (all of the numbers in the first category have a
		3 in the tens place). Sorting numbers by their divisibility
	Connections: M03-S1C1-02, M02-S1C2-04	can be used to reinforce multiplication and division facts.
		Examples:
		• Tarin drew the cards 4, 26, 18, 102, 75, 60, and 55 from a deck of cards labeled with the
		numbers 1 through 120. He sorted the cards
		and Group 2: 75, 55.
		 What categories might Tarin have used to sort the cards?
		• Where would you place the card 57 if it were drawn next?
		 The numbers 1-20 can be sorted into numbers that have a factor of 3 and numbers that have a
		factor of 4. NOTE: 12 would belong in both sets.
PO 5. Express benchmark fractions as fair sharing, parts of a	M03-S5C2-05. Represent a	Benchmark fractions include common fractions between
whole, or parts of a set.	problem situation using any	0 and 1 such as halves, thirds, fourths, fifths, sixths,
	combination of words, numbers,	eighths and tenths. Students are not expected to
Lesson 12 (squares into two & four equal parts)	pictures, physical objects, or	compute equivalent fractions but they should recognize
Lesson 17 (identity haives, iourins, eignins)	symbols.	that fractions can have more than one name.
Lesson 24 (write fractions using a fraction bar)	Connectiona: M03 S1C1 06	Examples:
Lesson 25-2 (writing fraction number sentences)	M03-S1C2-03	 Amy has 12 pencils. She is going to share the
Lesson 26 (writing fraction to show part of a set)	100-0102-00	pencils fairly among 3 people. What fraction of
Lesson 54 (measuring line segments to the nearest half inch)		the pencils will each person get?
Lesson 61 (fractions that show part of a set)		Continued on next page
Lesson 73 (adding and subtracting fractions)		 What fraction of the rectangle is shaded? Write the fraction in numerals and words. How might

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: Lesson 74 (adding and subtracting fractions) Lesson 78 (writing money/checks using fractions) Lesson 93 (compare, order, add and subtract fractions) Lesson 94 (fractions that equal ½, comparing fractions) Lesson 97 (showing time to the quarter hour) Lesson 98 (mixed numbers) Lesson 99 (quarter hours and inches) Lesson 111 (fractional parts of a set) Lesson 119 (tenth of a cm) Lesson 131 (common and decimal fractions)		you draw the rectangle in another way but with the same fraction shaded? $\boxed{\begin{array}{c} \hline \\ \hline $

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 6. Compare and order benchmark fractions. Lesson 25-2 (writing fraction number sentences) Lesson 26 (writing fractions to show part of a set) Lesson 54 (measuring line segments to nearest ½ inch) Lesson 60-2 (measuring with cups) Lesson 61 (part of a set) Lesson 73 & 74 (w/ denominators of 2, 3 & 6) Lesson 93 (w/ denominators 2, 3, 4 & 8) Lesson 94 (w/ denominators 2, 3, 4 & 8) Lesson 94 (w/ denominators 2, 3, 4, 5, 6, 8 & 10) Lesson 98 (mixed numbers) Lesson 99 (quarter inch) Lesson 111 (fractional part of a whole) Lesson 119 (tenth of a cm) Lesson 131 (common and decimal fractions)	M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection. Connections: M03-S1C1-05, M03-S1C3-01	Benchmark fractions include common fractions between 0 and 1 such as halves, thirds, fourths, fifths, sixths, eighths, and tenths. Fractions can be compared using benchmarks, common denominators, or common numerators. Symbols used to describe comparisons include $<, >, =, \neq$. Fractions may be compared using $\frac{1}{2}$ as a benchmark. • • • • • • • • • • • • • • • • • • •

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
	M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection.	Fractions with common denominators may be compared using the numerators as a guide. • $\frac{2}{6} < \frac{3}{6} < \frac{5}{6}$ Fractions with common numerators may be compared and ordered using the denominators as a guide. • $\frac{3}{10} < \frac{3}{8} < \frac{3}{4}$

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Grade 3

Strand 1: Number and Operations Concept 2: Numerical Operations

Understand and apply numerical operations and their relationship to one another.

In Grade 3, students build on their previous work with numbers to understand the meanings of multiplication and division. Students apply basic multiplication facts and efficient procedures. They explore the relationship between multiplication and division as they learn related multiplication and division facts.

Performance Objectives	Process Integration &	Explanations and Examples
	<u>Connections</u>	
Students are expected to:		
PO 1. Add and subtract whole numbers to four digits. Lesson 10-1 (subtraction facts) Lesson 11 (acting out subtraction story problems) Lesson 38 (adding three or more 1-digit numbers) Lesson 50-2 (making shape for given perimeter) Lesson 52 (adding 2-digit numbers) Lesson 67 (subtracting 2-digit numbers)	M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection. M03-S5C2-05. Represent a problem situation using any combination of words, numbers,	 Problems should include vertical and horizontal forms, including opportunities to apply the commutative and associative properties. Example: Mary read 1,173 pages over her summer reading challenge. She was only required to read 899 pages. How many extra pages did
Lesson 69 (add multiples of 100) Lesson 76 (add 3-digit numbers) Lesson 86 (colving larger/smaller/difference problems)	pictures, physical objects, or symbols.	Mary read over the challenge requirements?
Lesson 89 (sum of three addends) Lesson 91 & 92 (subtract 2- & 3-digit numbers) Lesson 96 (subtracting money amounts—checking answer) Lesson 102 (making change for \$1) Lesson 106 (adding money amounts to \$99,999.99) Lesson 126 (subtracting on a number line)	M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question.	Continued on next page
	Connections: M03-S1C1-01, M03-S1C1-03, M03-S1C2-02, M03-S1C3-01, M03-S2C1-02, M03-S2C4-02, M03-S2C4-03, M03-S3C1-01, M03-S3C1-02, M03-S3C2-01, M03-S3C3-01	

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Grade 3

Performance Objectives	Process Integration &	Explanations and Examples
	Connections	
Students are expected to:		
		 Students may solve the problem using the traditional algorithm. Here are four other methods students may use to solve the computation in the problem above. 899 + 1 = 900, 900 + 100 = 1,000, 1000 + 173 = 1,173, therefore 1+ 100 + 173 = 274 pages (Adding Up Strategy) 900 + 100 is 1,000; 1,000 + 173 is 1,173; 100 + 173 is 273 plus 1 (for 899, not 900) is 274 (Compensating Strategy) Take away 173 from 1,173 to get to 1,000, take away 100 to get to 900, and take away 1 to get to 899. Then 173 +100 + 1 = 274 (Subtraction Strategy) 899 + 1 is 900, 900, 1,000 (that's 100). 1,000, 1,100 (that's 200 total). 1,100, 1,110, 1,120, 1,130, 1,140, 1,150, 1,160, 1,170, (that's 70 more), 1,171, 1,172, 1,173 (that's 3 more) so the total is 1+200+70+3 = 274 (Adding by Tens or
PO 2. Create and solve word problems based on addition, subtraction, multiplication, and division.	M03-S5C2-05. Represent a problem situation using any	Students use a variety of representations for creating and solving one-step word problems, i.e.,
Math Meeting "Problem of the Day" in Lessons 1-135 Lesson 1 (elapsed time) Lesson 11 (addition and subtraction story problems) Lesson 35-2 (some/some more, some/some went away stories) Lesson 49 (finding perimeter) Lesson 50-2 (making shape for given perimeter) Lesson 52 (adding menu items) Lesson 56 (number sentences for equal groups) Lesson 57 (equal group stories)	combination of words, numbers, pictures, physical objects, or symbols. Connections: M03-S1C1-03, M03-S1C2-01, M03-S1C2-03, M03-S1C2-04, M03-S1C2-05, M03-S1C2-06, M03-S1C2-07, M03-S1C3-01, M03-S2C1-02, M03-S2C3-01, M03-S2C3-02, M03-S2C4-02, M03-S2C4-03, M03-S3C1-01, M03-S3C2-01.	numbers, words, pictures, physical objects, or equations. Students explain their thinking, show their work by using at least one of these representations, and verify that their answer is reasonable.

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Grade 3

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: Lesson 59 (identifying quotients) Lesson 65-2 (time on recipe) Lesson 66 (missing addend in some, some more stories) Lesson 67 (subtracting 2 digit numbers) Lesson 76 (adding 3 digit numbers) Lesson 82 (adding money amounts) Lesson 86 (larger-smaller-difference problems) Lesson 96 (subtracting money amounts—checking answer) Lesson 102 (making change for \$1) Lesson 106 (adding money amounts to \$99,999.99)	Connections M03-S3C3-02, M03-S3C3-03, M03-S4C4-01, M03-S4C4-03, M03-S4C4-03, M03-S4C4-05	
Lesson 122 (dividing with mental computation) Lesson 126 (adding, subtracting, multiplying on number line) Lesson 127 (finding distance on a map) Lesson E (choose an appropriate method to solve a problem)		

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 3. Demonstrate the concept of multiplication and division using multiple models. Lesson 37 (half of a set of objects) Lesson 45-1 (multiplying by 1 & 10) Lesson 55-1 (X7 facts) Lesson 56 (number sentences for equal groups) Lesson 57 (number sentences for equal groups) Lesson 59 (writing division problems in three ways) Lesson 63 (perfect squares, exponents) Lesson 70 (X2 facts) Lesson 81 (square roots of perfect squares) Lesson 84 (number of days in a year) Lesson 85-1 (X0, X5) Lesson 87 (make/draw arrays) Lesson 90 (dividing by 2, dividing by 5) Lesson 90 (division story problems) Lesson 103 (multiply by 100, by 1000) Lesson 107 (division story problems) Lesson 108 (division story problems) Lesson 112 (multiplying with mental computation) Lesson 113 (associative property of multiplication) Lesson 114 (associative property of multiplication) Lesson 122 (dividing with mental computation) Lesson 121 (finding volume) Lesson 122 (dividing with mental computation) Lesson 124 (multiplying on the number line) Lesson 135 (estimating by sampling)	 M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection. M03-S5C2-04. Determine whether a problem to be solved is similar to previously solved problems, and identify possible strategies for solving the problem. M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. Connections: M03-S1C1-01, M03-S1C1-05, M03-S1C2-02, M03-S1C2-04, M03-S1C2-05, M03-S1C2-06, M03-S2C3-01, M03-S2C3-02, M03-S3C3-03, M03-S4C4-04 	 Students are expected to be familiar with multiple representations. The equation 3 x 4 = 12 could be represented in the following ways. an array: an array: equal sets: <

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Grade 3

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
		Students should experience problems that involve both sharing and measurement.
		 Examples: This is an example of a partitive division or fair sharing problem: The bag has 92 hair clips, and Laura and her three friends want to share them equally. How many hair clips would each person get?
		 The following is an example of a measurement or repeated subtraction problem: Max the monkey loves bananas. Molly, his trainer, has 24 bananas. If she gives Max 4 bananas each day, how may days will the bananas last?
		Starting Day Da
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Arizona Department of Education: Standards and Assessment	Division	Solution: The bananas will last for 6 dates.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 4. Demonstrate fluency of multiplication and division facts through 10. Lesson 45-1 (factors & products) Lesson 55-1 (x7) Lesson 59 (divide by 10, by 7 & by 1) Lesson 70-1 (X2) Lesson 85-1 (x0, x5) Lesson 90 (dividing by 2, dividing by 5) Lesson 95-1 (x3) Lesson 100-1 (x4) Lesson 105-1 (multiplication/division fact families) Lesson 105-1 (multiplication/division fact families) Lesson 110-1 (X9) Lesson 112 (multiplying with mental computation) Lesson 115-1 (X6) Lesson 116 (multiplying with the multiplication algorithm) Lesson 120-2 (factors, prime numbers) Lesson 122 (dividing with mental computation) Lesson 125-1 (dividing by 6, 8, 9 fact families) Lesson 132 (division with remainders)	Connections: M03-S1C2-02, M03-S1C2-03, M03-S1C2-05, M03-S1C2-06, M03-S1C2-07, M03-S2C3-01, M03-S2C3-02, M03-S3C1-01, M03-S3C1-02, M03-S3C2-01, M03-S3C3-03	 Students demonstrate fluency with multiplication facts through 10 and the related division facts. Fact fluency includes working with facts flexibly, accurately, and efficiently. This means that students have quick recall using strategies that are efficient. Strategies for learning facts include: Zeros and Ones Doubles (2s facts), Doubling twice (4s), Doubling three times (8s) Tens Facts Five Facts (half of tens) Skip Counting (counting groups of) Square Numbers (Ex: 3 x 3) Nifty Nines Turn-around Facts (Commutative Property) Fact Families (Ex: 6 x 4 = 24; 24 ÷ 6 = 4; 24 ÷ 4 = 6; 4 x 6 = 24) Missing Factors Students may be able to master multiplication facts more easily if they can relate new facts to prior knowledge. When students think about 6 X 8, they might think about the familiar fact of 5 X 8. They know 5 X 8 = 40, so then they add 8 more to 40. They arrive at the answer of 48.

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols.	Multiplication and division facts are inverse operations and that understanding can be used to solve the unknown. Fact family triangles demonstrate the inverse operations of multiplication and division by showing the four possible facts using the same three numbers.
	Connections: M03-S1C2-02, M03-S1C2-03, M03-S1C2-04, M03-S1C2-06, M03-S3C3-03	Examples: • 3 x 5 = 15 5 x 3 = 15 • 15 ÷ 3 = 5 15 ÷ 5 = 3
		15 x or ÷ 3 5
PO 6. Describe the effect of operations (multiplication and division) on the size of whole numbers. Lesson 56, 57 (number sentences for equal groups) Lesson 63 (perfect squares, exponents) Lesson 81 (square roots of perfect squares) Lesson 84 (number of days in a year) Lesson 87 (make/draw arrays) Lesson 103, 109 (X10, X100, X1000) Lesson 107, 108 (division story problems) Lesson 112 (multiplying with mental computation) Lesson 116 (multiplying with the multiplication algorithm) Lesson 118 (associative property of multiplication) Lesson 122 (dividing with mental computation)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions. M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the	Multiplying whole numbers causes the quantity to increase. Dividing whole numbers causes the quantity to decrease. It is important to note that this is true for whole numbers, but not necessarily for all numbers.

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
Lesson 125-1 (determining unit cost) Lesson 126 (multiplying on the number line) Lesson 130-2 (large numbers)	Connections: M03-S1C2-02, M03-S1C2-03, M03-S1C2-04, M03-S1C2-05, M03-S1C3-01	
PO 7. Apply commutative, identity, and zero properties to multiplication and apply the identity property to division.	Connections: M03-S1C2-02, M03-S1C2-04	Properties of multiplication can be used to help remember basic facts.
Lesson 5 (commutative property of addition) Lesson 14 (adding 10, subtracting 10 using mental computation) Lesson 33 (adding a multiple of 10 using mental computation Lesson 35-2 (writing story problems using mental computation) Lesson 42 (adding 2-digit numbers using mental computation) Lesson 42 (adding 2-digit numbers using mental computation) Lesson 44 (identifying missing digit in addition problem) Lesson 45-1 (multiplicative identity) Lesson 56 (number sentences for multiplication) Lesson 59 (multiplicative identity) Lesson 59 (multiplicative identity) Lesson 105-1 (multiplication and division fact families) Lesson 112 (multiplying with mental computation) Lesson 116 (multiplying with multiplication algorithm) Lesson 133 (simplifying expressions to +, -, x, ÷) Lesson 135 (estimating by sampling)		 5 x 3 = 3 x 5 (Commutative Property) 1 x 5 = 5 or 5 x 1 = 5 (Identity Property) 12 ÷ 1 = 12 0 x 5 = 0 or 5 x 0 = 0 (Zero Property)

Strand 1: Number and Operations Concept 3: Estimation

Use estimation strategies reasonably and fluently while integrating content from each of the other strands.

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In Grade 3, students build upon their previous experience with estimation of numbers and quantities. They use multiple strategies to make estimations. Students compare the reasonableness of their estimate to the actual computation. Multiple and continuous estimation experiences lead to greater understanding of number sense.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Make estimates appropriate to a given situation or computation with whole numbers. Lesson 18 & 19 (rounding to nearest 10) Lesson 31 (estimating sums, mental computation of sums) Lesson 32 (estimate, draw & measure to nearest cm) Lesson 45-2 (estimate & find capacity) Lesson 46 (estimating reasonable temperature) Lesson 46 (estimating reasonable temperature) Lesson 50-2 (estimating length) Lesson 50-2 (estimate to verify calculated results) Lesson 52 (estimate to verify calculated results) Lesson 53 (estimate to verify calculated results) Lesson 55-2 (estimating capacity) Lesson 62 (estimate differences) Lesson 72 (estimate 3-digit sums/differences) Lesson 76 (adding 3-digit numbers) Lesson 85-2 (estimate & find area) Lesson 95-2 (estimate weight and mass) Lesson 121 (finding volume) Lesson 134 (place value to millions) Lesson D (predict relative size of solutions)	 M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection. M03-S5C2-04. Determine whether a problem to be solved is similar to previously solved problems, and identify possible strategies for solving the problem. M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question. 	Students estimate using all four operations with whole numbers. Students will also use estimation to compare fractions using benchmark fractions. Estimation strategies for comparing fractions extend from students' work with whole numbers. Estimation skills include identifying when estimation is appropriate, determining the level of accuracy needed, selecting the appropriate method of estimation, and verifying solutions or determining the reasonableness of situations using various estimation strategies. Continued on next page Estimation strategies include, but are not limited to: front-end estimation with adjusting (using the highest place value and estimating from the front end making adjustments to the estimate by taking into account the remaining amounts), clustering around an average (when the values are close together an average value is selected and multiplied by the number of values to determine an estimate), rounding and adjusting (students round down or round up and then adjust their estimate depending on how much the rounding affected the original values),

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
		 using friendly or compatible numbers such as factors (students seek to fit numbers together - i.e., rounding to factors and grouping numbers together that have round sums like 100 or 1000), and using benchmark numbers that are easy to compute (students select close whole numbers for fractions or decimals to determine an estimate). Specific strategies also exist for estimating measures. Students should develop fluency in estimating using standard referents (meters, yard, etc) or created referents (the window would fit about 12 times across the wall).

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Grade 3

Strand 2: Data Analysis, Probability, and Discrete Mathematics

This strand requires students to use data collection, data analysis, statistics, probability, systematic listing and counting, and the study of graphs. This prepares students for the study of discrete functions as well as to make valid inferences, decisions, and arguments. Discrete mathematics is a branch of mathematics that is widely used in business and industry. Combinatorics is the mathematics of systematic counting. Vertex-edge graphs are used to model and solve problems involving paths, networks, and relationships among a finite number of objects.

Concept 1: Data Analysis (Statistics)

Understand and apply data collection, organization, and representation to analyze and sort data.

In Grade 3, students construct and analyze frequency tables, single bar graphs, and single line graphs in addition to pictographs and tally charts from previous grades and use them to solve problems. Students' understanding of number and operations are reinforced as they interpret information from the displays of data.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Collect, record, organize, and display data using frequency tables, single bar graphs, or single line graphs. Lesson 2 (graphing data on a bar graph) Lesson 30-2 (tallying) Lesson 40-2 (draw a pictograph) Lesson 55-2 (bar graph w/ scale of 2) Lesson 70-2 (line graph) Lesson 80-2 (probability bar graph)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. Connections: M03-S1C1-01, M03-S2C1-02, SC03-S1C2-04, SC03-S1C2-05, SC03-S1C3-01, SS03-S4C1-05, SS03-S4C6-02	Single bar graphs should be created horizontally as well as vertically. Determining appropriate scale and units should be emphasized and provides an opportunity to reinforce multiplication and division skills. The construction and interpretation of data displays can be reinforced during social studies and science.
 PO 2. Formulate and answer questions by interpreting and analyzing displays of data, including frequency tables, single bar graphs, or single line graphs. Lesson 2 (reading a graph) Lesson 30-2 (collecting data and tallying) Lesson 40-2 (conducting a survey) 	M03-S5C2-01. Analyze a problem situation to determine the question(s) to be answered. M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions.	

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Lesson 55-2 (drawing bar graph) Lesson 70-2 (drawing line graph) Lesson 80-2 (collecting and analyzing data) Lesson 134 (place value to millions) Lesson A (identify mode, range, and median of a set of data) Lesson B (identify mean of a set of data)	M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question.	
	Connections: M03-S1C1-02, M03-S1C2-01, M03-S1C2-02, M03-S1C3-01, M03-S2C1-01, SC03-S1C1-02, SC03-S1C3-02, SC03-S1C3-03, SS03-S4C1-02	

Strand 2: Data Analysis, Probability, and Discrete Mathematics Concept 2: Probability

Understand and apply the basic concepts of probability.

In Grade 3, there are no performance objectives in this concept. Performance objectives begin in Grade 4.

Strand 2: Data Analysis, Probability, and Discrete Mathematics Concept 3: Systematic Listing and Counting

Understand and demonstrate the systematic listing and counting of possible outcomes.

In Grade 3, students use lists and charts to systematically organize information and determine the outcomes of a given situation.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Represent all possibilities for a variety of counting problems using arrays, charts, and systematic lists; draw conclusions from these representations.	M03-S5C2-0 5. Represent a problem situation using words, numbers, pictures, physical	After students solve many of these types of counting problems, they should begin to organize their initial random enumeration of possibilities into a systematic

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
Lesson 22 (organized lists) Lesson 34 (listing combinations) Lesson 50-1, 100-1 (make an organized list) Lesson 79 (selecting coins for given amounts) Lesson 80-2 (probability bag)	objects, or symbols. Connections: M03-S1C2-02, M03-S1C2-03, M03-S1C2-04, M03-S2C3-02, SC03-S1C2-05	 way of counting possibilities, particularly through the organization of information in a chart (array) or systematic list. Ultimately, students should begin to make connections to the multiplication principle of counting. See the examples below. Continued on next page Examples: Jan is hungry for a snack. A snack consists of one drink and one fruit. List all possible snacks that Jan could eat? <u>Drink</u> <u>Fruit</u> Milk Apple Juice Banana A Systematic List Milk-Apple (MA), Milk-Banana (MB), Juice-Apple (JA), Juice-Banana (JB) A Chart (Array) <u>Drink</u> Milk Juice Fruit Milk Juice Apple MA JA JA Banana MB JB List all the different two-topping pizzas that a customer can order from a pizza shop that only offers four toppings: pepperoni, sausage, mushroom-Onion Mushroom-Pepperoni Mushroom-Sausage

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: PO 2. Solve a variety of problems based on the multiplication principle of counting. Lesson 22 (organized lists) Lesson 34 (listing combinations) Lesson 50-1, 100-1 (make an organized list) Lesson 79 (selecting coins for given amounts) Lesson 80-2 (probability bag) Lesson 89 (sum of 3 addends)	M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection. M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question. Connections: M03-S1C2-02, M03-S1C2-03, M03-S1C2-04,	Onion-Pepperoni Onion-Sausage Pepperoni-Sausage • A Chart (Array) • A La chart (Array) • A chart (Array)
	M03-S1C3-01, M03-S2C3-01	

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Strand 2: Data Analysis, Probability, and Discrete Mathematics Concept 4: Vertex-Edge Graphs

Understand and apply vertex-edge graphs.

In Grade 3, students expand upon their previous experience with coloring pictures and maps in second grade to include more complex maps. Students should be able to justify how they know they used the least number of colors. Students learn that a street map can be represented by a vertex-edge graph and that routes can be represented by paths in graphs.

Performance Objectives	Process Integration &	Explanations and Examples
	<u>oonneetions</u>	
Students are expected to:		
PO 1. Color complex maps using the least number of colors	M03-S5C2-03. Select and use	Students should be given many opportunities to explore
and justify the coloring.	one or more strategies to	and color different types of maps and make conjectures
Nationality defined in Sover Math 2. The Four Color	efficiently solve the problem and	about patterns they notice.
Theorem could be easily addressed within Lesson 125-2	Justity the selection.	
"I ocating Information on a Map"	M03-S5C2-04. Determine	
	whether a problem to be solved	Continued on next page
For additional information, we recommend you go to the origin	is similar to previously solved	
of Arizona's discrete math standard at	problems, and identify possible	Examples:
http://dimacs.rutgers.edu/lp/institutes/dm.html	strategies for solving the	County map of Arizona
	problem.	Map of United States
	M03-S5C2-08 Make and test	
	conjectures based on data (or	
	information) collected from	
	explorations and experiments.	
	Connectione: 0002 0404 04	
	Connections: 5503-54C1-01	
PO 2. Investigate properties of vertex-edge graphs	M03-S5C2-02. Identify relevant,	It is very important to give students multiple
 circuits in a graph, 	missing, and extraneous	opportunities to find paths and circuits in graphs, before
weights on edges, and	information related to the solution	adding weights to the graphs. Once weights are added

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
 shortest path between two vertices. 	to a problem.	to the graphs, students can reinforce their addition skills.
Not addressed in Saxon Math-3.	M03-S5C2-04. Determine	In social studies, students construct maps of familiar
For additional information, we recommend you go to the origin	whether a problem to be solved	places. These maps can easily be connected to vertex-
of Arizona's discrete math standard at	problems and identify possible	euge graphs.
http://dimacs.rutgers.edu/lp/institutes/dm.html	strategies for solving the problem.	Definitions of properties of vertex-edge graphs include:
	M03-S5C2-05. Represent a	 path – connected sequence of edges that starts at a vertex and ends at a vertex
	problem situation using any	 circuit in a graph – path that starts and ends at
	combination of words, numbers,	the same vertex
	symbols.	 weight on an edge – value (or some number of objects) placed along an edge in a vertex-edge
	M03-S5C2-06. Summarize	graph to represent some quantity such as distance, time, cost, or number of traffic lights
	mathematical information,	
	conclusions.	Continued on next page
	M03-S5C2-07. Analyze and	
	evaluate whether a solution is	Example:
	correct, and answers the	 What is the shortest path (in minutes) from home to school?
	question.	6
	Connections: M03-S1C1-02,	School Park
	M03-S1C2-01, M03-S1C2-02, SS3-S4C1-03	
		Pool
		7 14
		Home

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
		The weights (values) on the graph represent time in minutes. Example: • If Liz leaves her home and visits all the locations on the graph only once and then returns home, she has traveled a circuit. List all the possible circuits. Movie Store Bank Grocery Cleaners Office Drugstore

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:	M03 S5C2 01 Apolyzo a	
ro 5. Solve problems using venex-edge graphs.	problem situation to determine	How many different paths can be traveled from
Not addressed in <u>Saxon Math-3</u> .	the question(s) to be answered.	point A to point B based on the graph below?
For additional information, we recommend you go to the origin of Arizona's discrete math standard at <u>http://dimacs.rutgers.edu/lp/institutes/dm.html</u>	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols.	D C C
	M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions.	E B
	M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question.	This problem can be made more complex by adding weights to the edges and directing the students to find the shortest path. Addition skills can be reinforced with this type of activity.
	Connections: M03-S1C2-01, M03-S1C2-02, M03-S1C3-01, SS3-S4C1-03	

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Strand 3: Patterns, Algebra, and Functions

Patterns occur everywhere in nature. Algebraic methods are used to explore, model and describe patterns, relationships, and functions involving numbers, shapes, iteration, recursion, and graphs within a variety of real-world problem solving situations. Iteration and recursion are used to model sequential, step-by-step change. Algebra emphasizes relationships among quantities, including functions, ways of representing mathematical relationships, and the analysis of change.

Concept 1: Patterns

Identify patterns and apply pattern recognition to reason mathematically while integrating content from each of the other strands.

In Grade 3, students understand that logical patterns exist and are a regular occurrence in mathematics. Students recognize, extend, and generalize numerical sequences with both words and symbols.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Recognize, describe, extend, create, and find missing	M03-S5C2-06. Summarize	Working with missing terms in sequences provides an
terms in a numerical sequence.	mathematical information,	opportunity to reinforce addition, subtraction,
	explain reasoning, and draw	multiplication, and division facts.
"Pattern" activity in Math Meetings 1-135	conclusions.	
Lesson 3 (writing 2-digit numbers)		Examples:
Lesson 16 (writing the date with digits)	Connections: M03-S1C2-01,	• 3, , 9, 12, 15,
Lesson 63 (perfect squares)	M03-S1C2-02, M03-S1C2-04,	
Lesson 68 (writing numbers to 1000)	M03-S3C1-02, M03-S3C2-01,	• 80.72.64.
Lesson 69 (adding and subtracting multiples of 100)	M03-S4C1-01, SC03-S1C1-02	
Lesson 70-1 & 80-1 (looking for a pattern to solve a problem)		Possible descriptions for the second pattern include:
Lesson 75-2 (Roman numerals)		 Each number is 8 less than the previous
Lesson 87 (arrays)		number.
Lesson 117 (identifying function rule)		• The first term is 8 x 10 The second is 8 x 9 The
Lesson 128 (adding positive and negative numbers)		3 rd term is 8 x 8. So the next term must be
Lesson 129 (creating coordinate plane)		
Lesson 134 (place value to millions)		
Lesson 135 (estimating by sampling)		

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PO 2. Explain the rule for a given numerical sequence and	M03-S5C2-06. Summarize	Example:
verify that the rule works.	mathematical information,	 What is the rule for the pattern?
	explain reasoning, and draw	2, 4, 6, 8, 10,
"Pattern" activity in Math Meetings 1-135	conclusions.	o rule: add 2 to the previous term
Lesson 16 (writing date with digits)		\circ verification: 2 + 2 = 4, 4 + 2 = 6, 6 + 2 =
Lesson 63 (perfect squares)	Connections: M03-S1C2-01,	8
Lesson 68 (writing numbers to 1000)	M03-S1C2-04, M03-S1C3-01,	
Lesson 69 (adding and subtracting multiples of 100)	M03-S3C1-01, M03-S3C2-01,	
Lesson 70-1 & 80-1 (looking for a pattern to solve a problem)	M03-S4C1-01	
Lesson 75-2 (Roman numerals)		
Lesson 117 (identifying function rule)		

Strand 3: Patterns, Algebra, and Functions Concept 2: Functions and Relationships

Describe and model functions and their relationships.

In Grade 3, students build on the ideas of functions from second grade. Students focus on the relationship between two quantities and how different representations are related.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Recognize and describe a relationship between two quantities, given by a chart, table or graph, in which the quantities change proportionally, using words, pictures, or expressions.	M03-S5C2-02. Identify relevant, missing, and extraneous information related to the solution to a problem.	The relationship can be given by a table, model, or input/output (function) machine. Examples:
Math Meeting in Ls 118-135 Lessons 40-1, 70-1, 80-1, 110-1 (make a table to solve a problem) Lesson 117 (identifying function rule)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or	• What rule is shown by the input/output machine? $3 \rightarrow 12$ <u>In Out</u>

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: Lesson 129 (locating points on a coordinate plane) Lesson 130-1(graphing points on coordinate plane)	symbols. M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions. Connections: M03-S1C1-01, M03-S1C2-01, M03-S1C2-02, M03-S1C2-04, M03-S1C2-02, M03-S3C1-01, M03-S3C1-02, M03-S3C2-02, M03-S4C1-01	
PO 2. Translate between the different representations of whole number relationships, including symbolic, numerical, verbal, or pictorial. "Pattern" activity in Math Meetings 1-135	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions. Connections: M03-S3C2-01, M03-S3C3-02, M03-S3C2-01, SC03-S1C2-05, SC03-S1C3-02, SS03-S4C1-05	 Students can represent whole number functions using pictures, numbers, symbols, and words. Pictures Pictures A A A Continued on next page Symbols The number of points equals 5 x n (if n = the number of stars) Words Each star has 5 points. In order to figure out the total number of points, you multiply the number of stars by 5. Table Stars Number of Points

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Performance Objectives	Process Integration & Connections	<u>Explanat</u>	ions and E	<u>Examples</u>	
Students are expected to:					
			1	5	
			2	10	-
			3	15	-
			4	20	

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Strand 3: Patterns, Algebra, and Functions Concept 3: Algebraic Representations

Represent and analyze mathematical situations and structures using algebraic representations.

In Grade 3, students use a variety of representations to illustrate mathematical situations and relationships. These representations help students conceptualize ideas and solve problems.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: PO 1. Record equivalent forms of whole numbers to six digits by constructing models and using numbers. Lesson 41 (write 3-digit numbers in expanded form) Lesson 64 (3- and 4-digit numbers w/ base-10 blocks, models & pictures) Lesson 76 (adding 3-digit numbers) Lesson 104 (4-digit numbers in expanded form) Lesson 111 (age of coins) Lesson 112 (multiplying with mental computation) Lesson 124 (dividing 2-digit numbers) Lesson 134 (place value to millions)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. Connections: M03-S1C1-01, M03-S1C1-02, M03-S1C2-01	Students may use manipulatives, pictures, or symbols to model whole numbers and their equivalent forms. Examples: • 142,350 = 100,000 + 40,000 + 2,000 + 300 + 50 • 3 x 8 = 6 x 4 • 3 x 8 = 6 x 4 • 3 x 8 = 15 + 9 • 20 = 10 + 5 + 5; 10 x 2; 10 + 10, 5 x 4; 10 + 10, etc. • Base Ten Model: 231 2 - 100's; 3 -10's +1 or 23 - 10's + 1 • 10 • 0
Students are expected to: PO 1. Record equivalent forms of whole numbers to six digits by constructing models and using numbers. Lesson 41 (write 3-digit numbers in expanded form) Lesson 64 (3- and 4-digit numbers w/ base-10 blocks, models & pictures) Lesson 76 (adding 3-digit numbers) Lesson 104 (4-digit numbers in expanded form) Lesson 11 (age of coins) Lesson 112 (multiplying with mental computation) Lesson 124 (dividing 2-digit numbers) Lesson 134 (place value to millions)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. Connections: M03-S1C1-01, M03-S1C1-02, M03-S1C2-01	Students may use manipulatives, pictures, or symbols t model whole numbers and their equivalent forms. Examples: • 142,350 = 100,000 + 40,000 + 2,000 + 300 + 50 • 3 x 8 = 6 x 4 • 3 x 8 = 15 + 9 • 20 = 10 + 5 + 5; 10 x 2; 10 + 10, 5 x 4; 10 + 10, etc. • Base Ten Model: 231 $2 - 100$'s; $3 - 10$'s + 1 or $23 - 10$'s + 1

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		

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Performance Objectives	Process Integration &	Explanations and Examples
	Connections	
Students are expected to:		
PO 2. Use a symbol to represent an unknown quantity in a	M03-S5C2-05. Represent a	Example:
given context.	problem situation using any combination of words, numbers,	 Chen baked 25 crackers. His friend ate some of the crackers. Chen now has 9 crackers. 25 - A
Lesson 10 (identifying relative place value)	pictures, physical objects, or	
Lesson 11 (some/some more, some/some went away stories)	symbols.	
Lesson 35-2 (add/subtract number sentences)		
Lesson 44 (identifying missing digit in addition problem)	Connections: M03-S1C2-02,	
Lesson 50-2 (making a shape for a given perimeter)	M03-S3C2-02, M03-S3C3-03	
Lesson 51 (constructing number line)		
Lesson 59 (identifying quotients)		
Lesson 66 (some, some more stories)		
Lesson 79 (selecting coins)		
Lesson 80-2 (probability bag)		
Lesson 80 (larger-smaller-difference problems)		
Lesson 69 (sull of 5 addenus)		
DO 2 Create and solve simple one step equations that can	M02 SEC2 01 Apolyzo o	Studente may create story problems or equations. When
be solved using addition and multiplication facts	problem situation to determine	crafting story problems, students should carefully
be solved using addition and multiplication facts.	the question(s) to be answered	consider the question(s) to be asked and answered
Lesson 5 (identify missing addends)		
Lesson 15-1 (sums of 10)	M03-S5C2-05. Represent a	Examples:
Lesson 20-1 (fact families)	problem situation using any	Solve the equations below:
Lesson 30-1 (adding 3 & 4 facts)	combination of words, numbers,	$6 \times \Lambda = 24$
Lesson 40-1 (adding 7 & 8 facts)	pictures, physical objects, or	$a \times 2 \times 2 = 24$
Lesson 44 (identifying missing digit in addition problems)	symbols.	
Lesson 50-1 (subtracting number from 10 facts)		$78 + \Delta = 92$
Lesson 60-1 (subtract 2 facts)	Connections: M03-S1C2-02,	
Lesson 65-1 (subtract 3 & 4 facts)	M03-S1C2-03, M03-S1C2-04,	Rachel has 3 bags. There are 4 marbles in
Lesson 66 (missing addend in some, some more stories)	M03-S1C2-05, M03-S3C3-02	each bag. How many marbles does Rachel
Lesson 75-1 (subtracting 5 & 6 facts)		have altogether? $3 \times 4 = m$
Lesson 80-1 (subtracting 7, 8, & 9 facts)		
Lesson 101 (missing addend for sum of 100)		
Lesson 105-1 (multiplication/division fact families)		

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Strand 3: Patterns, Algebra, and Functions **Concept 4: Analysis of Change**

Analyze how changing the values of one quantity corresponds to change in the values of another quantity.

In Grade 3, there are no performance objectives in this concept. Performance objectives begin in Grade 4.

Strand 4: Geometry and Measurement

Geometry is a natural place for the development of students' reasoning, higher thinking, and justification skills culminating in work with proofs. Geometric modeling and spatial reasoning offer ways to interpret and describe physical environments and can be important tools in problem solving. Students use geometric methods, properties and relationships, transformations, and coordinate geometry as a means to recognize, draw, describe, connect, analyze, and measure shapes and representations in the physical world. Measurement is the assignment of a numerical value to an attribute of an object, such as the length of a pencil. At more sophisticated levels, measurement involves assigning a number to a characteristic of a situation, as is done by the consumer price index. A major emphasis in this strand is becoming familiar with the units and processes that are used in measuring attributes.

Concept 1: Geometric Properties

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Analyze the attributes and properties of 2- and 3- dimensional figures and develop mathematical arguments about their relationships.

In Grade 3, students describe, analyze, compare, and classify two-and three-dimensional shapes.

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 1. Describe sequences of 2-dimensional figures created	M03-S5C2-05. Represent a	Examples:
by increasing the number of sides, changing size, or changing orientation.	problem situation using any combination of words, numbers, pictures, physical objects, or	 Describe how the length and area of the figures shown below are changing.
"Patterns" in Math Meetings 1-135	symbols.	
	M03-S5C2-06. Summarize	
	mathematical information,	Side Length Area
The bulleted items within a performance objective indicate the s	specific content to be taught.	

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Porformance Objectives	Process Integration 8	Explanations and Examples
	<u>Frocess integration &</u>	
	Connections	
Students are expected to:		
	explain reasoning, and draw	
	conclusions.	
	Connections: M03-S3C1-01,	3 9
	M03-S3C1-02, M03-S3C2-01,	
	M03-S3C2-02, M03-S4C1-02,	
	M03-S4C2-01, M03-S4C4-04,	
	M03-S4C4-05	Continued on next page
		Evenue of descriptions. As the side length of the servers
		increases the grap increases
		• Describe the pattern shown in the figures.
		• Describe the pattern shown in the figures.
		$\left \begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$
PO 2. Recognize similar figures.	MU4-S5C2-04. Determine	At this level students can only determine if a figure
	whether a problem to be solved	appears to be similar by observing the attributes. They

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
Lesson 20-2 (naming and drawing polygons) Lesson 48 (horizontal, vertical, oblique lines) Lesson 113 (naming triangles by their angles) Lesson 115-2 (identifying geometric solids)	 is similar to previously solved problems, and identify possible strategies for solving the problem. M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions. Connections: M03-S4C1-01 	need multiple opportunities to evaluate figures in different orientations. Example: • Which of the figures shown below are similar? How do you know?
PO 3. Identify and describe 3-dimensional figures including their relationship to real world objects: sphere, cube, cone, cylinder, pyramids, and rectangular prisms. Lesson 115-2 (identifying geometric solids)	M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions. Connections: M03-S4C1-04	

Strand 4: Geometry and Measurement Concept 2: Transformation of Shapes

Apply spatial reasoning to create transformations and use symmetry to analyze mathematical situations.

In Grade 3, students begin to apply their understanding of spatial reasoning and recognize how the positions of 2-dimensional figures change in terms of translations, reflections, and rotations.

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Students are expected to:		
 PO 1. Identify a translation, reflection, or rotation and model its effect on a 2-dimensional figure. Lesson 12 (congruent shapes) Lesson 110-2 (identifying translation, rotation & reflection) Meeting 116 Meeting 117 	 M03-S5C2-06. Summarize mathematical information, explain reasoning, and draw conclusions. M03-S5C2-08. Make and test conjectures based on data (or information) collected from explorations and experiments. Connections: M03-S4C1-01, M03-S4C2-02 	Students recognize that the shape remains the same when translated, reflected, or rotated. Translation (Slide) Reflection (Flip)
		Rotation (Turn)-Shape moves about a point

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<u>Connections</u>	
103-S5C2-06. Summarize nathematical information, xplain reasoning, and draw onclusions. 103-S5C2-08. Make and test onjectures based on data (or iformation) collected from xplorations and experiments.	Students need experiences with figures which are symmetrical and non-symmetrical. Figures include both regular and non-regular polygons. Folding cut-out figures will help students determine whether a figure has one or more lines of symmetry.
10: nat on 10: on 10: on 10: on	nnections 3-S5C2-06. Summarize hematical information, lain reasoning, and draw clusions. 3-S5C2-08. Make and test jectures based on data (or irmation) collected from lorations and experiments.

Strand 4: Geometry and Measurement Concept 3: Coordinate Geometry

Specify and describe spatial relationships using rectangular and other coordinate systems while integrating content from each of the other strands.

In Grade 3, there are no performance objectives in this concept. Performance objectives begin in Grade 4.

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Strand 4: Geometry and Measurement Concept 4: Measurement

Understand and apply appropriate units of measure, measurement techniques, and formulas to determine measurements.

In Grade 3, students form an understanding of perimeter and area. They select appropriate units, strategies, and tools to solve problems involving perimeter and area. In upper grades, they will calculate area and perimeters of more complex figures.

Performance Objectives	<u>Process Integration &</u> Connections	Explanations and Examples
Students are expected to:		
 PO 1. Determine elapsed time across months using a calendar by hours and half hours using a clock. 	M03-S5C2-01. Analyze a problem situation to determine the question(s) to be answered.	
Lesson 1 (to the hour, elapsed time) Lesson 4 (to the half hour) Lesson 16 (writing date w/ digits) Lesson 39 (to five-minute intervals, a.m. & p.m.) Lesson 55 (X7 facts, number of weeks) Lesson 71 (to the minute)	M03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection. M03-S5C2-05. Represent a	
Lesson 84 (days in each month, days in a year) Lesson 91 "The Meeting" Lesson 97 (to the quarter hour)	problem situation using any combination of words, numbers, pictures, physical objects, or symbols.	
	M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question.	
	Connections: M03-S1C2-02, M03-S1C3-01	

The bulleted items within a performance objective indicate the specific content to be taught.

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Grade 3

Performance Objectives	Process Integration & Connections	Explanations and Examples
Performance Objectives Students are expected to: PO 2. Apply measurement skills to measure length, weight, and capacity using US Customary units. Lesson 6 (drawing congruent line segments) Lesson 7 (measuring length and width) Lesson 32 (measuring line segments in cm) Lesson 43 (naming line segments) Lesson 45-2 (cup, pint, quart, gallon, liter) Lesson 49 (finding perimeter) Lesson 50-2 (making a shape for a given perimeter)	Process Integration & ConnectionsM03-S5C2-03. Select and use one or more strategies to efficiently solve the problem and justify the selection.M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols.	Explanations and Examples Measurement skills include: • selecting appropriate unit of measure • selecting the appropriate tool, and • estimating, measuring, and comparing estimate to actual measure.
Lesson 50-2 (making a snape for a given perimeter) Lesson 54 (drawing line segments to nearest half inch) Lesson 55-2 (estimating capacity) Lesson 60-2 (cups, tablespoons, teaspoons) Lesson 76 (adding 3-digit numbers) Lesson 85-2 (measuring in feet, yards, and meters) Lesson 88 (estimate & find area) Lesson 95-2 (ounces, pounds, tons, grams, kilograms Lesson 99 (measuring to nearest quarter inch) Lesson 114 (measuring with mm) Lesson 119 (tenth of a cm) capacity/volume – liters Lesson 121 (volume of rectangular prism) Lesson 130-2 (estimating large numbers) Lesson 134 (place value to millions) Lesson 135 (estimating by sampling)	M03-S5C2-08. Make and test conjectures based on data (or information) collected from explorations and experiments Connections: M03-S1C3-01, M03-S4C4-03, M03-S4C4-05, SC03-S1C2-04	
 PO 3. Convert units of length, weight, and capacity inches or feet to yards, ounces to pounds, and cups to pints, pints to quarts, quarts to gallons. 	M03-S5C2-02. Identify relevant, missing, and extraneous information related to the solution to a problem.	
Lesson 45-2 (cup, pint, quart gallon)	M03-S5C2-07. Analyze and	

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 Grade 3

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
Lesson 60-2 (cups, ½ cup, ¼ cup) Lesson 85-2 (feet, yards, meters) Lesson 95-2 (ounces, pounds, tons, grams, kilograms) Lesson 114 (measuring using mm) Lesson 119 (tenth of a cm)	evaluate whether a solution is reasonable, is mathematically correct, and answers the question.	
Lesson 127 (feet in mile, km to mile)	Connections: M03-S1C2-02, M03-S1C3-01, M03-S4C4-02	

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Grade 3

Performance Objectives	Process Integration &	Explanations and Examples
Students are expected to:		
Students are expected to: PO 4. Determine the area of a rectangular figure using an array model. Lesson 43 (area of a square) Lesson 63 (area of a square) Lesson 87 (make/draw arrays) Lesson 88 (estimate/find area)	M03-S5C2-05. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. M03-S5C2-07. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question. Connections: M03-S1C2-02, M03-S1C2-03, M03-S1C3-01, M03-S4C1-01, M03-S4C4-05	Students should be able to determine the possible rectangles with a given area. Examples: Array models can assist students with understanding square numbers. Students should recognize that a square is also composed of two rectangles. • $4 \times 4 = (2 \times 4) + (2 \times 4)$ • $4 \times 4 = (2 \times 4) + (2 \times 4)$ • A rectangle with an area of 24 could be arrays of 1×24 , 2×12 , 3×8 , 4×6 , 2×12 , 3×8 , 4×6 . • $6 \times 12 = (6 \times 10) + (6 \times 2)$ • $6 \times 12 = (6 \times 10) + (6 \times 2)$
	M03-S4C1-01, M03-S4C4-05	• A rectangle with an area of 24 could be arrays of 1 x 24, 2 x 12, 3 x 8, 4 x 6, 2 x 12, 3 x 8, 4 x 6. • 6 X 12 = (6 X 10) + (6 X 2) • $6 = \frac{10}{6 \times 10} = \frac{2}{60}$ • 6 groups of 10 6 groups of 2

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:		
PO 5. Measure and calculate perimeter of 2-dimensional figures.	M03-S5C2-04. Determine whether a problem to be solved is similar to previously solved	Students may use objects to represent length, such as string. A shape can be outlined with string and stretched into a straight line. The length can be
Lesson 49 (find perimeter) Lesson 50-2 (making a shape for a given perimeter)	problems, and identify possible strategies for solving the problem.	measured with a ruler. This reinforces the concept that perimeter is a linear measure.
	Connections: M03-S1C2-02, M03-S1C3-01, M03-S4C1-01, M03-S4C4-02, M03-S4C4-04	

Strand 5: Structure and Logic

This strand emphasizes the core processes of problem solving. Students draw from the content of the other four strands to devise algorithms and analyze algorithmic thinking. Strand One and Strand Three provide the conceptual and computational basis for these algorithms. Logical reasoning and proof draws its substance from the study of geometry, patterns, and analysis to connect remaining strands. Students use algorithms, algorithmic thinking, and logical reasoning (both inductive and deductive) as they make conjectures and test the validity of arguments and proofs. Concept two develops the core processes as students evaluate situations, select problem solving strategies, draw logical conclusions, develop and describe solutions, and recognize their applications.

Concept 1: Algorithms and Algorithmic Thinking

Use reasoning to solve mathematical problems.

In Grade 3, there are no performance objectives in this concept. Performance objectives begin in Grade 4.

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Grade 3

Strand 5: Structure and Logic Concept 2: Logic, Reasoning, Problem Solving, and Proof

Evaluate situations, select problem-solving strategies, draw logical conclusions, develop and describe solutions, and recognize their applications.

In Grade 3, students describe, explain, and justify their solution processes which may include numbers, words (including mathematical language), pictures, physical objects, or equations. Students use all of these representations as needed. For a particular solution, students should be able to explain or show their work using at least one representation and verify that their answer is reasonable.

Performance Objectives	Process Integration &	Explanations and Examples
	Connections	
Students are expected to:	Some of the Strand 5 Concept 2 performance objectives are listed throughout the grade level document in the Process Integration Column (2nd column). Since these performance objectives are connected to the other content strands, the process integration column is not used in this section next to those performance objectives.	
PO 1. Analyze a problem situation to determine the question(s) to be answered.		
Lesson 20-1 (used logical reasoning) Lessons 20-1, 90-1, 120-1 (work backwards) Lessons 30-1, 60-1, 90-1(guess and check) Lesson 35-2 (story problems for addition and subtraction) Lessons 40-1, 70-1, 80-1(draw a picture) Lessons 40-1, 70-1, 80-1, 100-1 (make a table) Lessons 50-1, 100-1 (make an organized list) Lessons 60-1, 80-1, 110-1, 130-1 (make it simpler) Lessons 70-1, 80-1 (look for a pattern) Lessons 107 & 108 (division story problems)		

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Grade 3

Performance Objectives	Process Integration &	Explanations and Examples
	<u>Connections</u>	
Students are expected to:	Some of the Strand 5 Concept 2 performance objectives are listed throughout the grade level document in the Process Integration Column (2nd column). Since these performance objectives are connected to the other content strands, the process integration column is not used in this section next to those performance objectives.	
DO 2 Identify relevant missing and extremestic		Any time students encrease a problem they should
 PO 2. Identify relevant, missing, and extraneous information related to the solution to a problem. Math Meeting "The Problem of the Day" in Lessons 1-135 Lesson 20-1 (used logical reasoning) Lessons 20-1, 90-1, 120-1 (work backwards) Lessons 30-1, 60-1, 90-1(guess and check) Lesson 35-2 (story problems for addition and subtraction) Lessons 40-1, 70-1, 80-1(draw a picture) Lessons 40-1, 70-1, 80-1, 100-1 (make a table) Lessons 50-1, 100-1 (make an organized list) Lessons 60-1, 80-1, 110-1, 130-1 (make it simpler) Lessons 70-1, 80-1 (look for a pattern) Lessons 107 & 108 (division story problems) 		Any time students approach a problem, they should consider what information is most important and decipher how the information is related to the question to be answered.
PO 3. Select and use one or more strategies to efficiently solve the problem and justify the selection. Math Meeting "The Problem of the Day" in Lessons 1-135 Lesson 20-1 (used logical reasoning) Lessons 20-1, 90-1, 120-1 (work backwards) Lessons 30-1, 60-1, 90-1(guess and check) Lesson 35-2 (story problems for addition and subtraction)		Students should be exposed to multiple problem-solving strategies and be able to choose which ones to use.

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Grade 3

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: Lessons 40-1, 70-1, 80-1(draw a picture) Lessons 40-1, 70-1, 80-1(draw a picture) Lessons 40-1, 70-1, 80-1, 100-1 (make a table) Lessons 50-1, 100-1 (make an organized list) Lessons 60-1, 80-1, 110-1, 130-1 (make it simpler) Lessons 70-1, 80-1 (look for a pattern) Lessons 107 & 108 (division story problems)	Some of the Strand 5 Concept 2 performance objectives are listed throughout the grade level document in the Process Integration Column (2nd column). Since these performance objectives are connected to the other content strands, the process integration column is not used in this section next to those performance objectives.	
PO 4. Determine whether a problem to be solved is similar to previously solved problems, and identify possible strategies for solving the problem. Daily expectation throughout <u>Saxon Intermediate 4</u> Beginning with the "Focus on Problem Solving" – pages 1-8 Specifically addressed by the daily "Problem Solving" activities provided in the "Power-Up" box.		This problem-solving process should be continuously reinforced throughout instruction. This will help students connect to prior learning and consider which problem- solving strategy might be more efficient in a particular case.

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Performance Objectives	Process Integration &	Explanations and Examples
	Connections	
Students are expected to:	Some of the Strand 5 Concept 2 performance objectives are listed throughout the grade level document in the Process Integration Column (2nd column). Since these performance objectives are connected to the other content strands, the process integration column is not used in this section next to those performance objectives.	
PO 5. Represent a problem situation using any combination of words, numbers, pictures, physical objects, or symbols. <i>Daily expectation throughout</i> <u>Saxon Intermediate 4</u> Beginning with the "Focus on Problem Solving" – pages 1-8 Specifically addressed by the daily "Problem Solving" activities provided in the "Power-Up" box.		
PO 6. Summarize mathematical information, explain reasoning, and draw conclusions.		Summarizing information, explaining your thinking, and drawing logical conclusions are all interconnected and difficult tasks for students to accomplish. These process
Math Meeting "The Problem of the Day" in Ls 1-135 Lesson 20-1 (used logical reasoning) Lesson s 20-1, 90-1, 120-1 (work backwards) Lesson 22 (making organized lists) Lesson s 30-1, 60-1, 90-1(guess and check) Lesson 35-2 (story problems for addition and subtraction) Lesson s 40-1, 70-1, 80-1(draw a picture) Lesson s 40-1, 70-1, 80-1, 100-1 (make a table) Lesson s 40-1, 70-1, 80-1, 100-1 (make a table) Lesson s 50-1, 100-1 (make an organized list) Lesson s 60-1, 80-1, 110-1, 130-1 (make it simpler) Lesson 70-1, 80-1 (look for a pattern)		skills form the foundation of "doing" mathematics and should be encouraged from a very young age.

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Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to: Lesson 79 (selecting coins)	Some of the Strand 5 Concept 2 performance objectives are listed throughout the grade level document in the Process Integration Column (2nd column). Since these performance objectives are connected to the other content strands, the process integration column is not used in this section next to those performance objectives.	
Lesson 86 (solving larger-smaller-difference problems) Lesson 90-2 (determine likelihood of event) Lesson 107 & 108 (division story problems) Lesson 134 (place value to millions) Lesson 135 (estimating by sampling)		
PO 7. Analyze and evaluate whether a solution is reasonable, is mathematically correct, and answers the question. Daily expectation throughout <u>Saxon Intermediate 4</u> Beginning with the "Focus on Problem Solving" – pages 1-8 Specifically addressed by the daily "Problem Solving" activities provided in the "Power-Up" box.		Students often do not check their solutions or evaluate whether their answers make sense. These processes should become common practice for efficient problem- solvers.
PO 8. Make and test conjectures based on data (or information) collected from explorations and experiments. <i>Daily expectation throughout</i> <u>Saxon Intermediate 4</u> Beginning with the "Focus on Problem Solving" – pages 1-8 Specifically addressed by the daily "Problem Solving" activities provided in the "Power-Up" box.		Making and testing conjectures closely connects to M03- S5C2-06 and these are all critical processes to help students create meaning.

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Grade 3

Performance Objectives	Process Integration & Connections	Explanations and Examples
Students are expected to:	Some of the Strand 5 Concept 2 performance objectives are listed throughout the grade level document in the Process Integration Column (2nd column). Since these performance objectives are connected to the other content strands, the process integration column is not used in this section next to those performance objectives.	

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Grade 3