

## AP ENVIRONMENTAL SCIENCE MATH AND EQUATION REVIEW

1) **Show all work.** No work, no credit. This is critically important for every calculation, even if it seems trivial.

2) **Show all units.** Units provide valuable information.

3) **Develop good “math sense” or “math literacy.”** The answers should make sense. If you calculate a cost of \$50 billion per gallon of water, does this seem right?

4) **Know simple conversion factors** such as the number of days in a year or hours in a day. Other good numbers to know:

U.S. population = approx. 300 million (300,000,000 or  $3 \times 10^8$ )

World population = approx. 6.8 billion (6,800,000,000 or  $6.8 \times 10^9$ )

5) **Know and convert metric prefixes.**

- T tera-  $10^{12}$  (trillion 1,000,000,000,000)
- G giga-  $10^9$  (billion 1,000,000,000)
- M mega-  $10^6$  (million 1,000,000)
- k kilo-  $10^3$  (1000)
- h hecto-  $10^2$  (100)
- da deka-  $10^1$  (10)
- d deci-  $10^{-1}$  (0.1)
- c centi-  $10^{-2}$  (0.01)
- m milli-  $10^{-3}$  (0.001)
- $\mu$  micro-  $10^{-6}$  (one-millionth 0.000001)
- n nano-  $10^{-9}$  (one-billionth 0.000000001)

6) **Be comfortable working with negative numbers.** Going from  $-8^\circ\text{C}$  to  $+2^\circ\text{C}$  is a  $10^\circ$  change.

7) **Use dimensional analysis.** Conversions should show units of measurement and conversion factors. Example: If water has a density of 62 pounds per cubic foot, how many tons of water are contained in a 4000 cubic foot tank?

4000 cubic foot tank x (62 pounds/cubic foot) x (1 ton/2000 pounds) = 132 tons

Example: If electricity costs \$0.20 per kilowatt hour, calculate the cost to run a 1500 watt appliance for two hours.

1500 watts x (1 kilowatt/1000 watts) x 2 hours x (\$0.20/kilowatt hour) = \$0.60

8) **Work scientific notation problems without a calculator.** Multiplication and division will be common. Multiplying numbers in scientific notation requires the exponents to be added. Dividing numbers in scientific notation requires exponents to be subtracted.

Examples:  $10^6 \text{ TIMES } 10^3 = 10^9$

$10^8 \text{ DIVIDED BY } 10^1 = 10^7$

9) **Calculate percent change.** Percent change can be calculated by finding the difference between the old and new values, and then dividing by the old value. Convert to a percent by multiplying by 100.

Example: old value = \$400, new value = \$500, percent change =  $(\$100/\$400) \times 100 = 25\%$  increase

10) **Calculate population growth rate and population density.** Growth rate =  $[b - d] + [i - e]$   
Population density = population divided by area

11) **Know the Rule of 70 to predict doubling time.**  
Doubling time = 70 divided by annual growth rate (in %)

12) **Calculate half-life.**

AMOUNT REMAINING = (ORIGINAL AMOUNT)(0.5)<sup>x</sup>  
where x = number of half-lives

13) **Calculate pH using  $-\log [H^+]$ .**  $\log_{10} x = y$  and  $10^y = x$ .  
Most pH problems are easily solved without a calculator. Remember that for every one-increment change in pH, the ion concentrations change by a factor of 10.

Examples: if pH = 6, then the concentration of hydrogen ions  $[H^+] = 1 \times 10^{-6}$   
If pH = 2, then the concentration of hydrogen ions  $[H^+] = 1 \times 10^{-2}$   
If the concentration of hydrogen ions =  $1 \times 10^{-13}$ , then the pH = 13

14) **Be familiar with units of energy and power.**

- Watt = joule/sec = volts x amps
- Calorie = energy to raise one gram of water by one degree C.
- BTU (British thermal unit) = energy to raise one pound of water by one degree F.
- Kilowatts x hours = kilowatt hours
- Efficiency = energy out divided by energy in

15) **AP GRAPHING TIPS**

- Label each axis.
- Set both axes to scale with consistent increments.
- Connect dots.
- Interpolate and extrapolate.
- Be comfortable with doing graphs by hand.
- Include a title and a key.