

2.5 Linear Equations

Day 2 (1)


Slope-intercept $y = mx + b$

Point-slope $y - y_1 = m(x - x_1)$

Standard Form $Ax + By = C$

slope = $m = \frac{y_2 - y_1}{x_2 - x_1}$

If $m = \frac{1}{2}$
 $m_{\text{parallel}} = \frac{1}{2}$
 $m_{\text{perpendicular}} = -\frac{2}{1}$



90° opposite reciprocal

$x = 4$ vertical \updownarrow slope is undefined

$y = 4$ horizontal \leftrightarrow slope = \emptyset

Ex 6 Write an equation in slope-intercept and standard form that passes through $(3, 5)$ and ...

(a) is parallel to $2x + 5y = 4$

What is the slope?

$$\begin{array}{r} -2x \qquad \qquad \qquad -2x \\ \hline \end{array}$$

$$\frac{5y}{5} = \frac{-2x + 4}{5}$$

$$y = -\frac{2}{5}x + \frac{4}{5}$$

slope = $-\frac{2}{5}$

$$2.5 \quad m = -\frac{2}{5} \quad \text{point } (x_1, y_1)$$

Day 2 (2)

Plug into point-slope

$$y - y_1 = m(x - x_1)$$

$$(5) \quad y - 5 = -\frac{2}{5}(x - 3)$$

$$5y - 25 = -2(x - 3)$$

$$5y - 25 = -2x + 6$$

$$\begin{array}{cccc} +2x & +25 & +2x & +25 \\ \hline \end{array}$$

$$\boxed{2x + 5y = 31}$$

Change to standard form

X and y same side

Convert to slope-intercept

$$y = mx + b$$

get y alone

$$\begin{array}{ccc} 2x + 5y = 31 \\ -2x & & -2x \\ \hline \end{array}$$

$$\frac{5y}{5} = -\frac{2x}{5} + \frac{31}{5}$$

$$\boxed{y = -\frac{2}{5}x + \frac{31}{5}} \leftarrow \text{slope-intercept form}$$

2.5

Ex 6 b

Find equation of line

Day 2 (3)

through point $(3, 5)$ and perpendicular to
 $2x + 5y = 4$ in slope-intercept and
 standard form.

$$m_{\parallel} = -\frac{2}{5}$$

$$m_{\perp} = \frac{+5}{2}$$

$Ax + By = C$
 Standard Form \rightarrow plug into point-slope

$$y - y_1 = m(x - x_1)$$

$$(2)y - 5^{(2)} = \frac{5}{2}(x - 3)$$

$$2y - 10 = 5(x - 3)$$

$$2y - 10 = 5x - 15$$

$$-5x + 10 - 5x + 10$$

\rightarrow Get x and y on
 same side

$$\boxed{-5x + 2y = -5}$$

$$\boxed{5x - 2y = 5}$$

Standard Form!

Slope-intercept

$$y = mx + b$$

get y alone

$$\begin{array}{r} -5x + 2y = -5 \\ +5x \qquad \qquad +5x \\ \hline \end{array}$$

$$\frac{2y}{2} = \frac{5x - 5}{2}$$

$$\boxed{y = \frac{5}{2}x - \frac{5}{2}}$$

Slope-intercept

Ex 7

x	Year	Cost (\$)
0	2009	6312
1	2010	6695
2	2011	7136
3	2012	7703
4	2013	8070

$x = 0$ represents 2009

a) Find equation

$(0, 6312)$ and $(4, 8070)$

$$m = \frac{8070 - 6312}{4 - 0} = \frac{1758}{4} = 439.5 = m$$

Slope indicates cost of tuition and fees increased by about \$440 each year from 2009 to 2013.

$$y = 439.5x + 6312$$

b) Estimate cost in 2015

$$x = \frac{2015}{-2009} = 6$$

$$y = 439.5(6) + 6312 = \boxed{\$8949}$$

↑
tuition in 2015